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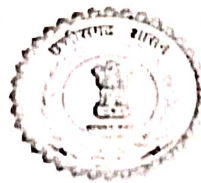
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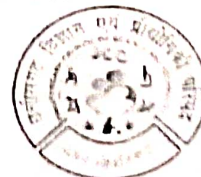


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SDIS-013

Performance Measures for a Three-Unit Compact Circuit

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**Abstract**

*This paper analyses a three component system with single repair facility. Denoting the failure times of the components as  $T_1$  and  $T_2$  and the repair time as  $R$ , the joint survival function of  $(T_1, T_2, R)$  is assumed to be that of trivariate distribution of Marshall and Olkin. Here,  $R$  is an exponential variable with parameter  $\alpha$  and  $T_1$  and  $T_2$  are independent of each other. In this paper use of Laplace-Transform is taken for finding Mean Time Between Failure, Availability and Mean Down Time and table for Reliability measure is shown in the end.*

**Key Words:** MTBF, Availability, MDT, Reliability.

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**[1] Introduction**

Reliability measures for a two-component standby system with repair facility were obtained by several authors under different assumptions in the past. Lie et al. (1977) and Yearout et al. (1986) have done extensive reviews for the failure times and repair times assuming that these are statistically independent. Joshi and Dharmadhikari (1989) considered the bivariate exponential distribution to derive the performance measures associated with a two-component standby system. Goel and Srivastava (1991) considered a correlated structure for the failure and repair times and obtained various reliability measures.

In many situations, a unit or system can be repaired immediately after breakdown. In such cases, the mean time between failures refers to the average time of breakdown until the device is beyond repair. When a system is often unavailable due to breakdowns and is put back into operation after each breakdown with proper repairs, the mean time between breakdowns is often defines as the mean time between failures. If we consider only active repair time i.e. the time spent for actual repair, then the mean time to repair (MTTR) is

the statistical mean time for active repair. It is the total active repair time during a given period divided by the number of during the same interval. Frequently, a system may be unavailable on account of periodic inspections and not because of breakdowns. By the systematic inspection or preventive maintenance for the detection of defects and prevention of failures, the system is kept in a satisfactory operational condition. The time spent for this is termed as the preventive maintenance downtime. There is difference between mean time between maintenance (MTBM) and mean time between failures (MTBF). When preventive maintenance downtime is zero or is not considered, MTBM is same as MTBF.

Here in this paper, we perform the analysis of a three-component standby system with single repair facility. Here  $T_1$  is the exponential variable with parameter  $k_1$  and  $T_2$  is another random variable with parameter  $k_2$ .  $R$  is an exponential variable with parameter  $\alpha$ .  $T_1$  and  $T_2$  are independent of each other. It is further assumed that these components are identical in nature and each unit works as new after the repair and switching devices are perfect and instantaneous.

The following are the assumptions for the model:

- (i) The system is composed of three components linked in parallel-series configuration (Fig. 1).
- (ii) The components are non-identical in nature.
- (iii) At time  $t=0$ , all the components are in operable mode.
- (iv) After repair each unit works as new.
- (v) Switching devices are perfect and instantaneous.

Define  $p_i(t) = \Pr\{X(t) = i : X(0) = 0\}, i = 0, 1, 2$

Here in this model, we consider the following trivariate exponential distribution for  $(T_1, T_2, R)$  with survival function of (Marshall and Olkin, 1967) of the form :

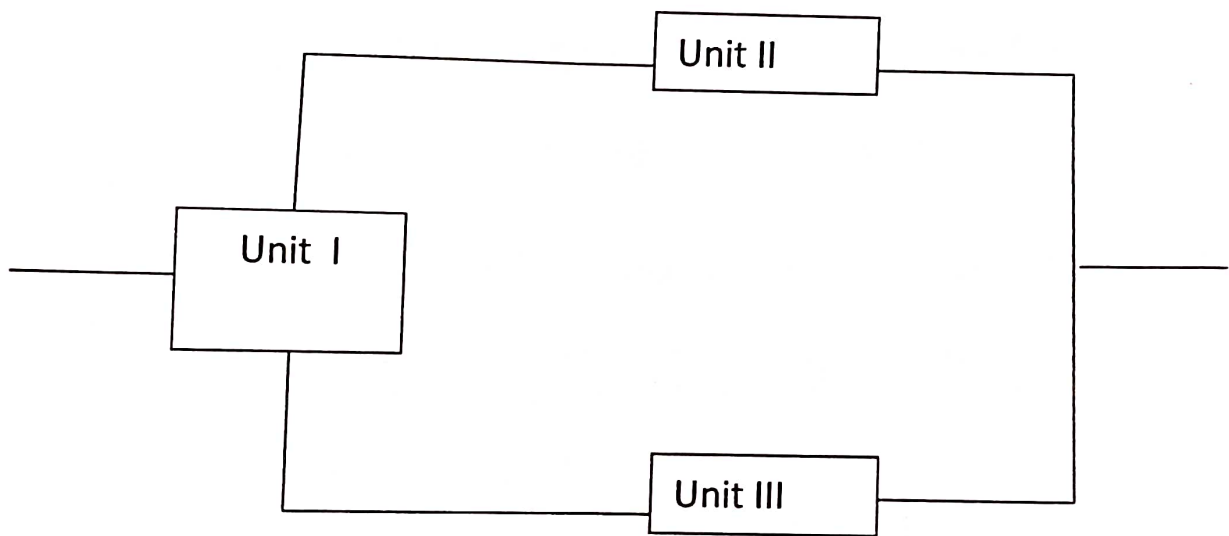
$$\bar{F}(t_1, t_2, t_3) = \exp[-k_1(t_1 + t_2) - k_2 t_3 - k_3 \{\max(t_1, t_2) + \max(t_2 + t_3)\}]$$

$$t_1, t_2, t_3 \geq 0; k_1, k_2 > 0; k_3 \geq 0 \quad [1.1]$$

It may be observed that

- i)  $T_1$  and  $T_2$  are independent and identically distributed exponential random variables with the parameter  $(k_1+k_2)$ ,
- ii)  $R$  is exponential with the parameter  $(k_2+2k_3)$ , not necessarily independent of  $(T_1, T_2)$  and
- iii)  $(T_1, R)$  and  $(T_2, R)$  are identically distributed as bivariate exponential with the parameter  $(k_1, k_2+k_3, k_3)$ .

By considering (1) as the survival function of  $(T_1, T_2, R)$  , we obtain expressions for reliability, MTBF and the gain due to repair facility. The state transition diagram for the system, in the interval  $(t, t + \Delta t)$  is given below:



**Figure 1 State Transition Diagram of three-unit standby System**

**[2] MTBF Calculation**

Since reliability of the system is given by  $R(t) = P_0(t) + P_1(t) + P_2(t)$ , we want to find the

expressions for  $P_0(t)$ ,  $P_1(t)$  and  $P_2(t)$ . We know that  $MTBF = \int_0^{\infty} R(t) dt$

We have,  $p_i(t) = p_r \{X(t) = i : X(0) = 0\}$ ,  $i = 0, 1, 2$

So,  $p_i(t + \Delta t) = p_r \{X(t + \Delta t) = i : X(0) = 0\}$

$$= \sum_{j=0}^2 p_r \{X(t + \Delta t) = 0, X(t) = j : X(0) = 0\}$$

Using  $P(AB) = P(A/B)P(B)$ , we have

$$= \sum_{j=0}^2 p_r \{X(t + \Delta t) = 0, X(t) = j\} \{X(t) = j : X(0) = 0\}$$

$$= \sum_{j=0}^2 p_r \{X(t + \Delta t) = 0, X(t) = j\} p_j(t)$$

$$= p_r \{X(t + \Delta t) = 0 : X(t) = 0\} p_0(t) + p_r \{X(t + \Delta t) = 0 : X(t) = 1\} p_1(t) \\ + p_r \{X(t + \Delta t) = 0 : X(t) = 2\} p_2(t)$$

$$p_0(t + \Delta t) = (1 - \alpha \Delta t) p_0(t) + \gamma \Delta t p_1(t) + 0(\Delta t)$$

$$p_0(t + \Delta t) - p_0(t) = -\alpha \Delta t p_0(t) + \gamma \Delta t p_1(t) + 0(\Delta t)$$

Dividing by  $\Delta t$  and taking limit  $\Delta t \rightarrow 0$  we have

$$\lim_{\Delta t \rightarrow 0} \frac{p_0(t + \Delta t) - p_0(t)}{\Delta t} = -\alpha p_0(t) + \gamma p_1(t) + \lim_{\Delta t \rightarrow 0} \frac{0(\Delta t)}{\Delta t}$$

$$p_0'(t) = -\alpha p_0(t) + \gamma p_1(t) \tag{2.1}$$

Similarly, we can write  $p_1(t + \Delta t) = pr(X(t + \Delta t) = 1 : X(0) = 0)$

$$p_1(t + \Delta t) = \sum_{j=0}^2 pr(X(t + \Delta t) = 1, X(t) = j : X(0) = 0)$$

$$= \sum_{j=0}^2 pr(X(t + \Delta t) = 1, X(t) = j) p_j(t)$$

$$= pr\{X(t + \Delta t) = 1 : X(t) = 0\} p_0(t) + pr\{X(t + \Delta t) = 1 : X(t) = 1\} p_1(t) \\ + pr\{X(t + \Delta t) = 1 : X(t) = 2\} p_2(t)$$

so, we have  $p_1(t + \Delta t) = \alpha \Delta t p_0(t) + \{1 - (\beta + \gamma) \Delta t\} p_1(t)$  which on simplification gives

$$p_1'(t) = \alpha p_0(t) - (\beta + \gamma) p_1(t)$$

Assuming,  $\alpha = k_1 + k_3$ ,  $\beta = k_1$  and  $\gamma = k_2 + k_3$ , we get the equations [6.2.3] and [6.2.4] in the following reduced form:

$$p_0'(t) = -(k_1 + k_3) p_0(t) + (k_2 + k_3) p_1(t)$$

$$p_1'(t) = (k_1 + k_3) p_0(t) - (k_1 + k_2 + k_3) p_1(t)$$

$$p_2'(t) = k_2 p_0(t) - (k_1 + k_2 + k_3) p_1(t) + k_2 p_2(t) \quad [2.2-2.4]$$

Taking Laplace transform on both the sides of [6.1.5] and [6.1.6] and noting that

$$L\{p_i(t)\} = L_i(s)$$

$$\text{We get } (k_1 + k_3 + s)L_0(s) - (k_2 + k_3)L_1(s) + (k_3 + s)L_2(s) = 1$$

$$(k_1 + k_3)L_0(s) - (k_1 + k_2 + k_3 + s)L_1(s) + k_2 L_2(s) = 0$$

$$\text{and } (k_2 + s)L_0(s) - (k_1 + s)L_1(s) + (k_1 + k_3 + s)L_2(s) = 0$$

solving using Cramer rule, we get

$$L_0(s) = \frac{(k_1 + k_2 + k_3 + s)}{\{s^2 + (2k_1 + k_2 + 2k_3)s + k_1(k_1 + k_3)\}}$$

$$L_1(s) = \frac{(k_1 + k_3)}{\{s^2 + (2k_1 + k_2 + 2k_3)s + k_1(k_1 + k_3)\}} \text{ and}$$

$$L_2(s) = \frac{(k_2 + k_3 + s)}{\{s^2 + (2k_1 + k_2 + 2k_3)s + k_1(k_1 + k_3)\}}$$

Let  $s_1$  and  $s_2$  be the roots of the equation  $s^2 + (2k_1 + k_2 + 2k_3)s + k_1(k_1 + k_3) = 0$

$$\text{let } s_1 = \frac{-(2k_1 + k_2 + 2k_3) + \sqrt{k_2^2 + 4(k_1 + k_3)(k_2 + k_3)}}{2} \quad [2.5-2.6]$$

$$\text{and } s_2 = \frac{-(2k_1 + k_2 + 2k_3) - \sqrt{k_2^2 + 4(k_1 + k_3)(k_2 + k_3)}}{2}$$

Since  $s_1, s_2 < 0$ . Thus we have,

$$L_0(s) = \frac{(k_1 + k_2 + k_3 + s)}{\{(s - s_1)(s - s_2)\}}; \quad L_1(s) = \frac{(k_1 + k_3)}{\{(s - s_1)(s - s_2)\}}; \quad L_2(s) = \frac{(k_2 + k_3 + s)}{\{(s - s_1)(s - s_2)\}}$$

Resolving into partial fractions, we have

$$L_0(s) = \frac{(k_1 + k_2 + k_3 + s_1)}{(s - s_1)(s_1 - s_2)} - \frac{(k_1 + k_2 + k_3 + s_2)}{(s - s_2)(s_1 - s_2)}$$

$$L_1(s) = \frac{(k_1 + k_3)}{\{(s - s_1)(s - s_2)\}}$$

$$L_2(s) = \frac{(k_2 + k_3)}{\{(s - s_1)(s - s_2)\}}$$

[2.7-2.9]

Taking inverse Laplace transforms of the above equations, we get

$$p_0(t) = \frac{(k_1 + k_2 + k_3 + s_1)e^{s_1 t} - (k_1 + k_2 + k_3 + s_2)e^{s_2 t}}{s_1 - s_2} \quad \text{and}$$

$$p_1(t) = \frac{(k_1 + k_3 + s_1)(e^{s_1 t} - e^{s_2 t})}{s_1 - s_2}$$

$$p_2(t) = \frac{(k_2 + k_3)(e^{s_1 t} - e^{s_2 t})}{s_1 - s_2}$$

[2.10-2.12]

Hence the reliability of the system is given by  $R(t) = p_0(t) + p_1(t) + p_2(t) = \frac{s_2 e^{s_1 t} - s_1 e^{s_2 t}}{s_1 - s_2}$



$$MTBF = \int_0^{\infty} R(t) dt = -\frac{(s_1 + s_2)}{s_1 s_2} \text{ where } s_1 \text{ and } s_2 \text{ are given by equation above.}$$

$$\text{So, } MTBF = \frac{(k_1 + k_2 + 2k_3)}{k_1(k_1 + k_3)} \quad [2.11]$$

it may be noted that MTBF when there is no repair facility is given by

$$MTBF (\text{no repair facility}) = E(T_1 + T_2) = E(T_1) + E(T_2) = \frac{1}{k_1 + k_3} + \frac{1}{k_1 + k_3} = \frac{2}{k_1 + k_3} \quad [2.12]$$

### [3] Availability analysis of the system

In this section, we consider the transient solution of the system and the availability measures such as the point wise availability and the steady-state availability by considering the above model. By considering the equation [1.1] as the survival function of  $(T_1, T_2, R)$ , we obtain the expressions for point wise availability and the steady-state availability. Using similar arguments as in the case of MTBF, we obtain the following differential equations:

$$p_0'(t) = -(k_1 + k_3)p_0(t) + (k_2 + k_3)p_1(t)$$

$$p_1'(t) = (k_1 + k_3)p_0(t) - (k_1 + k_2 + k_3)p_1(t) + (k_2 + 2k_3)p_2(t)$$

$$p_2'(t) = k_1 p_1(t) - (k_2 + 2k_3)p_2(t) \quad [3.1-3.3]$$

Taking Laplace transforms of above three equations and applying the Cramer's rule, we get

$$L_0(s) = \frac{s^2 + (k_1 + 2k_2 + 2k_3)s + (k_2 + k_3)(k_2 + 2k_3)}{s^3 + 2(k_1 + k_2 + 2k_3)s^2 + \{(k_1 + k_2 + 2k_3)^2 - k_1(k_2 + k_3)\}s}$$

$$L_1(s) = \frac{(k_1 + k_3)(k_2 + 2k_3 + s)}{s^3 + 2(k_1 + k_2 + 2k_3)s^2 + \{(k_1 + k_2 + 2k_3)^2 - k_1(k_2 + k_3)\}s} \text{ and}$$

$$L_2(s) = \frac{k_1(k_1 + k_2)}{s^3 + 2(k_1 + k_2 + 2k_3)s^2 + \{(k_1 + k_2 + 2k_3)^2 - k_1(k_2 + k_3)\}s} \quad [3.4-3.6]$$

Let  $s_1$  and  $s_2$  be the roots of the equation

$$s^2 + 2(k_1 + k_2 + 2k_3)s + (k_1 + k_2 + 2k_3)^2 - k_1(k_2 + k_3) = 0$$

Resolving into partial fractions, we have

$$L_0(s) = \frac{s_2\{s_1^2 + (k_1 + 2k_2 + 2k_3)s_1 + (k_2 + k_3)(k_2 + 2k_3)\}}{(s_1 - s_2)(s - s_1)s_1s_2} + \frac{s_1\{s_2^2 + (k_1 + 2k_2 + 2k_3)s_2 + (k_2 + k_3)(k_2 + 2k_3)\}}{(s_2 - s_1)(s - s_2)s_1s_2} + \frac{(k_2 + k_3)(k_2 + 2k_3)}{s s_1 s_2}$$

Similarly, we can write

$$L_1(s) = \frac{(k_1 + k_3)[s_2(k_2 + 2k_3 + s_1)]}{(s_1 - s_2)(s - s_1)s_1s_2} + \frac{s_1(k_2 + 2k_3 + s_2)}{(s_2 - s_1)(s - s_2)s_1s_2} + \frac{(k_2 + 2k_3)}{s s_1 s_2}$$

$$L_2(s) = \frac{s_2 k_1 (k_1 + k_3)}{(s_1 - s_2)(s - s_1)s_1s_2} + \frac{s_1}{(s_2 - s_1)(s - s_2)s_1s_2} + \frac{1}{s s_1 s_2}$$

[3.7- 3.8]

Taking Inverse Laplace transform on both the sides of equations [6.2.7-6.2.8], we get

$$p_0(t) = \frac{s_2 e^{s_1 t} \{s_1(s_1 + k_1 + 2k_2 + 3k_3) + (k_2 + k_3)(k_2 + 2k_3)\}}{s_1 s_2 (s_1 - s_2)} + \frac{s_1 e^{s_2 t} \{s_2(s_2 + k_1 + 2k_2 + 3k_3)(k_2 + k_3)(k_2 + 2k_3)\}}{s_1 s_2 (s_2 - s_1)} + \frac{(k_2 + k_3)(k_2 + 2k_3)}{s_1 s_2}$$

$$p_1(t) = \frac{s_2 e^{s_1 t} (s_1 + k_2 + 2k_3)(k_1 + k_3)}{s_1 s_2 (s_1 - s_2)} + \frac{s_1 e^{s_2 t} (s_2 + k_2 + 2k_3)(k_1 + k_3)}{s_1 s_2 (s_2 - s_1)} + \frac{(k_2 + 2k_3)}{s_1 s_2}$$

$$p_2(t) = \frac{s_2 e^{s_1 t} k_1 (k_1 + k_3)}{s_1 s_2 (s_1 - s_2)} + \frac{s_1 e^{s_2 t} k_1 (k_1 + k_3)}{s_1 s_2 (s_2 - s_1)} + \frac{k_1 (k_1 + k_3)}{s_1 s_2} \quad [3.9-3.11]$$

The point availability of the system is given as  $A(t) = p_0(t) + p_1(t) = 1 - p_2(t)$  i.e.

$$A(t) = 1 - \frac{s_2 e^{s_1 t} k_1 (k_1 + k_3)}{s_1 s_2 (s_1 - s_2)} + \frac{s_1 e^{s_2 t} k_1 (k_1 + k_3)}{s_1 s_2 (s_2 - s_1)} + \frac{k_1 (k_1 + k_3)}{s_1 s_2} \quad [3.12]$$

Thus the steady state availability of the system is given as

$$A_\infty = \lim_{t \rightarrow \infty} A(t) = 1 - \frac{k_1 (k_1 + k_3)}{s_1 s_2} = \frac{(k_2 + 2k_3)(k_1 + k_2 + 2k_3)}{(k_2 + 2k_3)^2 + k_1 (k_1 + k_2 + 3k_3)} \quad [3.13]$$

**[4] Mean Down Time Calculation:** The system mean down time is an important aspect of Availability analysis and is evaluated by the formula  $MDT = MTBF \left( \frac{1 - A_\infty}{A} \right)$ . So, using

the results from [3.10] and [3.13], we get

$$MDT = \frac{2k_1 + k_2 + 2k_3}{(k_1 + 2k_3)(2k_1 + k_2 + 2k_3)} \quad [4.1]$$

#### [5] References:

1. Nakagawa, T. and Osaki, S. [1976]. "Markov renewal process with some non-regenerative points and their applications to reliability". *Microelectronics Reliability*, 15(6), 633-636.
2. C.H. Lie, C.L. Hwang and F.A. Tillman [1977], "Availability of Maintained systems: A state of the art survey", *A.I.I.E. Trans.*, 9, 247-259.
3. Okumoto, K. [1985]. "Availability of 2-component dependent system". *IEEE Trans. On Reliability*, R-30(2) 205-210.
4. Yearout, R.D, Reddy P, Grosh DL [1986]. "Standby redundancy in reliability- a review". *IEEE Trans on Reliability*.
5. Joshi, B.H. and Dharmadhikari, A.D. [1989]. "Maximization of availability of 1 out-of-2 : G repairable dependent system". *Adv. Appl. Prob.* 21, 717-720.
6. Goel, L.R. and Srivastava, P. [1991]. "Profit analysis of a two-unit redundant system with provision for rest and correlated failure and repair". *M. & R.* 31 827-833.

7. Papageorgiou, Effii and Kokolakis, George[2004]. "A Two unit parallel system supported by (n-20 standbys with general and non-identical life times". *International Journal of System Science*,35(1) (2004), 1-12.
8. Singh,S.N. & Singh,S.K.[2007]. "A study on a two unit parallel system with Erlangian repair time", *Statistica (Bologona)*,67 (1) (2007), 69-77.
9. Wu,Qingtai, Zhang,Jin and Tang, Jiashan.[2015]. "Reliability evaluation for a class of multi unit cold standby systems under Poisson shocks". *Comm.Statist.Theory Methods* , 44(15) , 3278-3288.

**[6] Observation**

We provide the data in the following table. The table gives the values for MDT for various values for  $k_1$ ,  $k_2$  and  $k_3$ .

**Table 6.1**

$k_1$	$k_2$	$k_3$	$S_1$	$S_2$	$R(t)$
.01	0.1	.01	-5.984 -3.123 -2.136	-6.293 -5.603 -1.610	$12.992e^{-2t} - 10.526e^{-2.5t} - .02e^{-7.876t}$ $10.965e^{-4t} - 0.785e^{-6.5t} - .802e^{-4.976t}$ $9.095e^{-6t} - 0.584e^{-7.5t} - .04e^{-9.872t}$
.02	0.2	.02	-7.000 -6.667 -3.125	-6.177 -5.986 -2.955	$3.09e^{-2.07t} - 5.506e^{-2.5t} - .076e^{-6.874t}$ $2.654e^{-4.24t} - 1.085e^{-6.86t} - 2.202e^{-0.906t}$ $4.889e^{-6.76t} - 0.004e^{-2.56t} - 3.045e^{-6.952t}$
.03	0.3	.03	-6.875 -4.414 -3.250	-6.172 -4.133 -3.074	$4.225e^{-2.0t} - 3.793e^{-7.5t} - .068e^{-6.07t}$ $6.259e^{-7.25t} - 3.005e^{-2.85t} - 2.762e^{-0.006t}$ $7.809e^{-3.75t} - 0.974e^{-2.06t} - 0.049e^{-0.952t}$
.04	0.4	.04	-7.224 -4.454 -1.667	-6.179 -3.264 -1.633	$10.09e^{-5.07t} - 5.506e^{-2.5t} - .084e^{-0.874t}$ $12.690e^{-9.24t} - 7.025e^{-9.82t} - 9.002e^{-0.006t}$ $14.249e^{-0.76t} - 0.904e^{-8.56t} - 3.045e^{-6.952t}$

**[7] Declaration:** It is hereby declared that there is no conflict of interest among authors of this paper.