

BRAIN INTERNATIONAL SCHOOL

SUBJECT : MATHEMATICS

CLASS : XI

JUNE 2021

CHAPTER : SETS , RELATIONS AND FUNCTIONS

Q1. Describe the set $\{x \in N : x \text{ is a perfect square, } 10 < x < 20\}$ in Roster form.

Q2. Describe the set $\{-1, 1\}$ in set builder form.

Q3. Which of the following sets are disjoint :

$A = \{2, 1, 4\}$, $B = \{-1, 5, 1\}$, $C = \{1, 9\}$, $D = \{x \in N | x < 3\}$, $E = \{x : x \text{ is an odd natural number greater than } 3\}$.

Q4. State “True” or “False”, for each of the following :

- (i) $\{1\} \in \{1, 2, 3\}$
- (ii) $1 \in \{1, 2\}$
- (iii) $\{x \in N | x + 8 = 8\} \subseteq Z$
- (iv) $\{b, c\} \subset \{a, \{b, c\}\}$

Q5. Let $U = \{x \in N | x \leq 9\}$; $A = \{x : x \text{ is an even number, } 0 < x < 10\}$; $B = \{2, 3, 5, 7\}$
Verify that, $(A \cup B)' = A' \cap B'$.

Q6. Two finite sets have m and n elements. The total number of subsets of the first set is 112 more than the total number of subsets of the second set. The value of m and n are respectively

- (i) 4, 7
- (ii) 7, 4
- (iii) 4, 4
- (iv) 7, 7

Q7. Given set $A = \{1, 2, 3, 4, \dots, 100\}$.

- (i) Write the subset X of A, whose elements are multiples of 7.
- (ii) Write the subset Y of A, whose elements are represented by $x + 3$, when $n \in A$.

Q8. In a survey conducted on a group of 1800 people it is found that 1200 people liked product A and 900 people liked product B. What is the least number of people who liked both the products A and B, given that 500 people did not like any of the product.

Q9. In a survey of 25 students, it was found that 15 had taken Mathematics, 12 had taken Physics and 11 had taken Chemistry, 5 had taken Mathematics and Chemistry, 9 had taken Mathematics and Physics and 4 had taken Physics and Chemistry and 3 had taken all the three subjects. Find the number of students that had taken none of the subjects.

Q10. Given $R = \{(x, y) : y = x - 3, x, y \in Z\}$. State which of the ordered pairs belong to the relation

- (i) (5, 2)
- (ii) (1, 2)

- (iii) (0, -3)
- (iv) (7, -4)
- (v) (-4, 1)

Q11. Find domain and range of the relation R given by,

$$R = \left\{ (x, y) : y = x + \frac{6}{x}, xy \in N, x < 6 \right\}$$

Q12. If $(x - 1, y + 3) = (2, x + 4)$, find x and y .

Q13. Find the range of the function $(x) = \frac{|x-5|}{5-x}$.

Q14. If $A \times B = \{(a, 1), (a, 2), (b, 1), (b, 2)\}$. Find the sets A and B and hence find $B \times A$.

Q15. Let $A = \{1, 2, 3, 6, 9, 18\}$. Find the set R such that
 $R = \{(a, b) \mid a, b \in A \text{ and } a \text{ is a multiple of } b\}$.

Q16. Let $A = \{1, 2, 3\}$, $B = \{3, 4\}$ and $C = \{4, 5, 6\}$, find :

- (i) $A \times (B \cap C)$
- (ii) $(A \times B) \cup (A \times C)$

Q17. Re-define, the function given by $f(x) = |x - 1| + |1 + x|$, $-2 \leq x \leq 2$.

Q18. A relation R is defined on the set of integer as $R = \{(x, y) \mid x^2 + y^2 = 64\}$.

Q19. Let $f(x) = x^2 - x$ and $g(x) = x$ be two functions defined in the domain $R^+ \cup \{0\}$.
 Find

- (i) $(f + g)(0)$
- (ii) $(f - g)(-1)$
- (iii) $(fg)\left(\frac{1}{2}\right)$
- (iv) $\left(\frac{f}{g}\right)(4)$

Q20. Let $A = \{1, 2, 3\}$, $B = \{4\}$ and $C = \{5\}$, verify that, $A \times (B \cup C) = (A \times B) \cup (A \times C)$

Q21. Write the relation R in set $A = \{x \in Z, |x| \leq 5\}$, defined as
 $R = \{(a, b) \in A \times A \mid b = 2a + 3\}$. Find domain and range.