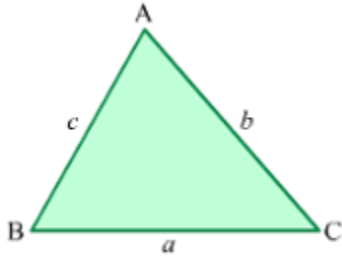


Heron's Formula

- **Perimeter** is the length of the boundary of a closed figure.
- The perimeter of a polygon is the sum of the lengths of all its sides.
In case of a triangle ABC, with sides of lengths a , b and c units:



Perimeter of ABC = AB + BC + AC = $a + b + c$

- The **semi-perimeter** of a triangle is half the perimeter of the triangle.

The semi-perimeter (s) of a triangle with sides a , b and c is $\frac{a+b+c}{2}$.

- The semi-perimeter of a triangle is used for calculating its area when the length of altitude is not known.

- **Area of triangle using Heron's formula:**

When all the three sides of a triangle are given, its area can be calculated using Heron's formula, which is given by:

$$\text{Area of triangle} = \sqrt{s(s-a)(s-b)(s-c)}$$

Here, s is the semi-perimeter of the triangle and is given by, $s = \frac{a+b+c}{2}$

Example: Find the area of a triangle whose sides are 9 cm, 28 cm and 35 cm.

Solution: Let $a = 9$ cm, $b = 28$ cm and $c = 35$ cm

$$\text{Semi-perimeter, } s = \frac{a+b+c}{2} = \frac{9+28+35}{2} \text{ cm} = 36 \text{ cm}$$

$$\text{Area of triangle} = \sqrt{36(36-9)(36-28)(36-35)} \text{ cm}^2$$

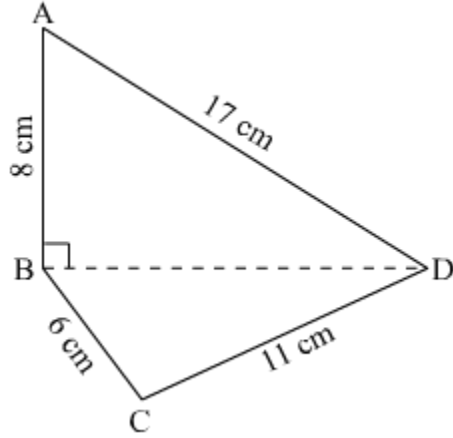
$$= \sqrt{36 \times 27 \times 8 \times 1} \text{ cm}^2$$

$$= 36\sqrt{6} \text{ cm}^2$$

- **Area of quadrilaterals using Heron's formula:**

Area of a quadrilateral can also be calculated using Heron's formula. In this, the quadrilateral is divided into two triangles and then the area of each triangle is calculated using Heron's formula.

Example: What is the area of the given quadrilateral?



Solution: $\triangle ABD$ is a right-angled triangle.

Using Pythagoras Theorem, we get

$$BD = \sqrt{(AD)^2 - (AB)^2} = \left(\sqrt{(17)^2 - (8)^2} \right) \text{cm} = 15 \text{ cm}$$

$$\text{Area} (\triangle ABD) = \frac{1}{2} \times \text{Base} \times \text{Height} = \frac{1}{2} \times 15 \times 8 = 60 \text{ cm}^2$$

For $\triangle BCD$, let $a = 6 \text{ cm}$, $b = 11 \text{ cm}$ and $c = 15 \text{ cm}$

$$\text{Semi-perimeter, } s = \frac{a+b+c}{2} = \left(\frac{6+11+15}{2} \right) \text{cm} = 16 \text{ cm}$$

$$\text{Area} (\triangle BCD) = \sqrt{s(s-a)(s-b)(s-c)}$$

$$= \sqrt{16(16-6)(16-11)(16-15)} \text{ cm}^2$$

$$= \sqrt{16 \times 10 \times 5 \times 1} \text{ cm}^2$$

$$= 20\sqrt{2} \text{ cm}^2$$

$$\text{Area of quadrilateral ABCD} = (60 + 20\sqrt{2}) \text{cm}^2 = 20(3 + \sqrt{2}) \text{ cm}^2$$