Roll No.

E-512

M. Sc. (Second Semester) (Main/ATKT) EXAMINATION, May-June, 2021

PHYSICS

Paper Second

(Statistical Mechanics)

Time: Three Hours [Maximum Marks: 80]

Note: Attempt all Sections as directed.

Section—A

1 each

(Objective/Multiple Choice Questions)

Note: Attempt all questions.

Choose the correct answer:

- 1. According to Liouville theorem the rate of change of density ρ of phase points in phase space is given by :
 - (a) $\frac{\partial \rho}{\partial t} = \infty$
 - (b) $\frac{\partial \rho}{\partial t} = 0$
 - (c) $\frac{\partial \rho}{\partial t}$ = negative
 - (d) $\frac{\partial \rho}{\partial t} = 1$

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2. In a canonical ensemble, the quantities same for each system are :

- (a) Temperature, volume and the number of particles
- (b) Energy, volume and the number of particles
- (c) Only energy
- (d) Only volume and the number of particles
- 3. The entropy of a system in an irreversible adiabatic process :
 - (a) Decreases
 - (b) Increases
 - (c) Unchanged
 - (d) Nothing can be said.
- 4. Four distinguishable coins are tossed many times. The most probable macrostate will be:
 - (a) 0, 4
 - (b) 1, 3
 - (c) 2, 2
 - (d) 3, 1
- 5. In a microcanonical ensemble, each system has the same :
 - (a) Energy and chemical potential
 - (b) Temperature and number of particles
 - (c) Temperature and chemical potential
 - (d) Energy and number of particles

- 6. Boltzmann's partition function z is:
 - (a) $e^{-\beta/\epsilon_r}$
 - (b) $\sum_{r} g_r e^{-\beta/\epsilon}$
 - (c) $\frac{\sum_{r} g_{r} e^{-\beta/\epsilon_{r}}}{\sum_{r} \epsilon_{r}}$
 - (d) $\frac{\sum_{r} \in_{r} g_{r} e^{-\beta/\epsilon_{r}}}{\sum_{r} g_{r} e^{-\beta/\epsilon_{r}}}$
- 7. Electrons obey:
 - (a) M. B. Statistics
 - (b) B. E. Statistics
 - (c) F. D. Statistics
 - (d) All of the above
- 8. Particles can be considered distinguishable if:
 - (a) $\frac{n_i}{g_i} \ll 1$
 - (b) $\frac{n_i}{g_i} >> 1$
 - (c) $\frac{n_i}{g_i} \lesssim 1$
 - (d) None of the above

- 9. Fermions are not:
 - (a) Molecules
 - (b) Electrons
 - (c) Protons
 - (d) Neutrons
- 10. Two particles obeying the Fermi-Dirac statistics are divided in 6 energy levels. The number of possible arrangements will be:

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- (a) 36
- (b) 15
- (c) 12
- (d) 8
- 11. The Brownian motion becomes more vigorous:
 - (a) When temperature is increased and viscosity of supporting fluid is decreased.
 - (b) When temperature is decreased and viscosity of supporting fluid is increased.
 - (c) When temperature and viscosity of supporting fluid is increased.
 - (d) None of the above
- 12. For Bose gas, the chemical potential $\boldsymbol{\mu}$ is always :
 - (a) Positive
 - (b) Zero
 - (c) Negative
 - (d) None of the above

- 13. He⁴ obeys the :
 - (a) B. E. Statistics
 - (b) F. D. Statistics
 - (c) M. B. Statistics
 - (d) None of the above
- 14. Liquid He II has:
 - (a) Low entropy and high viscosity
 - (b) Zero entropy and zero viscosity
 - (c) Zero entropy and low viscosity
 - (d) High entropy and high viscosity
- 15. It is possible from the study of Brownian motion to determine the value of :
 - (a) Avogadro number
 - (b) Boltzmann constant
 - (c) Both (a) and (b)
 - (d) None of the above
- 16. For a system with a large value of degree of freedom, the fluctuation is:
 - (a) Large
 - (b) Negligible
 - (c) Zero
 - (d) None of the above

17. Transition from non-ferromagnetic state to ferromagnetic state is a phase transition of :

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- (a) First order
- (b) Second order
- (c) Zero order
- (d) Not a phase transition
- 18. If D is coefficient of diffusion and B is mobility, then the correct form of Einstein relation in fluctuation is:
 - (a) $D = \frac{B}{kT}$
 - (b) D = B.kT
 - (c) $D = \frac{T}{kB}$
 - (d) None of the above
- 19. If ρ is the function of some property of the ensemble which is independent of time the ensemble is in :
 - (a) Thermal equilibrium
 - (b) Statistical equilibrium
 - (c) Mechanical equilibrium
 - (d) Particle equilibrium
- 20. The mean distance between molecular of a gas :
 - (a) Increases as density increases
 - (b) Decreases as density increases
 - (c) Increases with increasing temperature
 - (d) None of the above

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Section—B

2 each

(Very Short Answer Type Questions)

Note: Attempt all questions.

- 1. Explain phase space.
- 2. Define micro-canonical ensemble.
- 3. Explain macroscopic states.
- 4. Define energy fluctuations in the canonical ensemble.
- 5. Discuss the density of states.
- 6. Describe the property of ideal Fermi gas.
- 7. Define white dwarf stars.
- 8. Explain thermo-dynamic fluctuations.

Section—C

3 each

(Short Answer Type Questions)

Note: Attempt all questions.

- 1. Explain volume in phase space.
- 2. State the conditions of F. D. Statistics.
- 3. Explain contact between statistics and thermodynamics.
- 4. State and prove Liouville's theorem.
- 5. Explain electron gas in metals.
- 6. State the properties of liquid Helium II.
- 7. What do you understand by viral equation of state?
- 8. Discuss the density of states.

Section—D

5 each

P. T. O.

(Long Answer Type Questions)

Note: Attempt any *four* questions.

- 1. Explain phase space and quantum state. Obtain an expression for the volume element of the phase space and number of quantum states corresponding to this volume state.
- 2. Write in brief about partition function of canonical ensemble.

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- 3. Explain in brief Boltzmann's transport equation.
- 4. Write the difference between M. B., F. D. and B. E. Statistics.
- 5. What is degenerate electron gas? Calculate Fermi energy of degenerate electron gas.
- 6. State and prove fluctuation dissipation theorem.
- 7. What is Brownian motion? Discuss Einstein-Smoluchowski theory of Brownian motion.
- 8. Derive expression for the most probable distribution of particles according to Bose-Einstein's Statistics.